# A Bayesian Model to Estimate Male and Female Fertility Patterns at a Subnational Level

Riccardo Omenti <sup>1</sup> Monica Alexander <sup>2</sup> Nicola Barban <sup>1</sup>

<sup>1</sup>University of Bologna

<sup>2</sup>University of Toronto

September 11, 2024









## Importance of measuring male fertility

- ▶ Male fertility measurement is overlooked (Coleman 2000)
- ► Increasing involvement of men in fertility decisions (Lappegård et al. 2011)
- ➤ Trajectories in male fertility can differ systematically from those of women due to:
  - ▶ different reproductive age spans (Schoumaker 2019)
  - unbalanced sex ratios (Dudel & Klüsener 2016)
  - distinct cultural norms (Dudel & Klüsener 2021)

## Objectives

- ▶ Goal  $\rightarrow$  construction of a Bayesian model to estimate male and female period TFR at a subnational level
  - Essential component of population change
  - Shape local policies
- Data example → US counties during the period 1982-2019
  - ► High heterogeneity in fertility behaviors across time and space
  - High quality data registration systems

# Challenges

- Data on births disaggregated by paternal ages are often unavailable
  - Countries with inefficient data registration systems or lacking high quality surveys
  - Small regions with masked ages at childbearing due to privacy concerns
- Even in developed countries, birth registration systems have started recording childbearing ages of men quite recently
- ► The share of births with missing paternal ages is much higher than for maternal ages (Dudel & Klüsener 2016)

## Methodological Framework

Build on the Bayesian model by Schmertmann & Hauer (2019)

Idea  $\rightarrow$  Estimation of period Total Fertility Rate (TFR) without knowledge of births by maternal ages

#### **Data Requirements**

- Counts of children under 5
- Counts of women aged 15-49

#### Prior requirement

- Child mortality estimates
- Standard age-specific fertility schedules



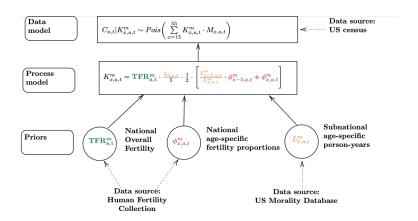
#### Proposed extension

Extend the previous Bayesian model to estimate male and female fertility at a subnational level

#### **Extensions**

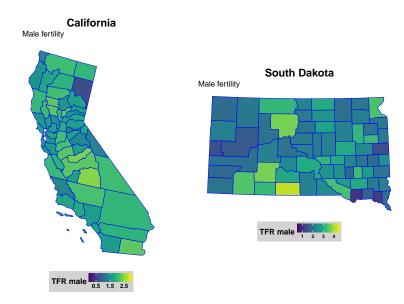
- ► Inclusion of men aged 15-59
- Incorporation of subnational mortality estimates
- ▶ Account for spatial dependencies → information pooling
- ► Account for temporal dependencies → temporal smoothing

## Bayesian model summary

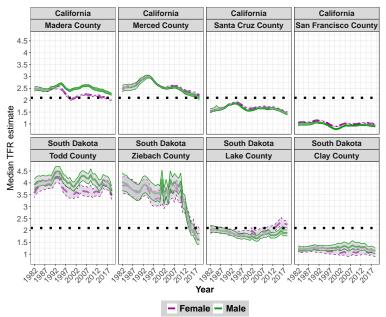


Final Goal $\rightarrow$  Draw samples from the marginal posterior distribution  $TFR_{a,t}^s|$  data, other parameters

#### California and South Dakota in 2015



#### Male and female TFR in selected counties



## Preliminary conclusions

- Using county-level population counts by age and sex allows to derive subnational period TFR estimates without the need of information on parental ages.
- No striking differences between male and female fertility
- Country-specific characteristics determine a high spatial heterogeneity and distinct temporal trajectories.

#### Future research

- Account for internal migration
- ► Test the model on other countries
- Better examine the relationship between sex-specific TFR and unbalanced sex ratios.

### Any Questions??

Looking forward to your feedback!

Contact: riccardo.omenti2@unibo.it

nomenti.github.io @OmentiRiccardo

Acknowledgements: ERC Grant GENPOP n. 865356

#### Essential Bibliography



Carl P Schmertmann and Mathew E Hauer.

Bayesian estimation of total fertility from a population's age—sex structure. Statistical Modelling, 19(3):225–247, 2019.



David A Coleman.

Male fertility trends in industrial countries: Theories in search of some evidence. International Union for the Scientific Study of Population, 1995.



Christian Dudel and Sebastian Klüsener.

Estimating male fertility in eastern and western germany since 1991: A new lowest low? Demographic Research, 35:1549–1560, 2016.



Bruno Schoumaker.

Male fertility around the world and over time: How different is it from female fertility? Population and Development Review, pages 459–487, 2019.



Christian Dudel, Yen-hsin Alice Cheng, and Sebastian Klüsener.

Shifting parental age differences in high-income countries: Insights and implications. *Population and Development Review*, 49(4):879–908, 2023.



Li Zhang.

Male fertility patterns and determinants, volume 27.

Springer Science & Business Media, 2010.

## Bayesian model

#### Data model:

$$C_{a,t}|K^s_{x,a,t} \sim \operatorname{Pois}\bigg(\sum_{x=15}^{\omega^s} K^s_{x,a,t} \cdot E^s_{x,a,t}\bigg)$$

$$K_{x,a,t}^{s} = TFR_{a,t}^{s} \cdot \frac{\tilde{L}_{0,a,t}}{5} \cdot \frac{1}{2} \cdot \left[ \frac{\tilde{L}_{x-5,a,t}^{s}}{\tilde{L}_{x,a,t}^{s}} \cdot \phi_{x-5,a,t}^{s} + \phi_{x,a,t}^{s} \right]$$

with  $w^F = 45$  and  $w^M = 55$ 

- ▶ Overall fertility  $(TFR_{a,t}^s)$
- lacktriangle Age- and sex-specific fertility proportions  $(\phi^s_{x,a,t})$
- ▶ Age- and sex-specific person-years  $(L_{x,a,t}^s)$

## Priors on fertility parameters

#### Prior on TFR

$$TFR_{a,t}^s \sim \mathcal{N}(TFR_t^{nat,s}, \sigma_{TFR_{a,t}^s}^2)$$

Prior on age-specific fertility patterns

$$\gamma_{x,a,t}^s = m_x^s + y_{1,x}^s \beta_{1,a,t}^s + y_{2,x}^s \beta_{2,a,t}^s$$

$$\gamma_{x,a,t}^s = \log\left(\frac{\phi_{x,a,t}^s}{\phi_{15,a,t}^s}\right)$$

Pooling information over countries

$$\beta_{p,a,t}^s \sim \mathcal{N}(\mu_{\beta_{p,t}^s}, \sigma_{\beta_{p,a,t}^s}^2)$$

Smoothing over time

$$\mu_{\beta_{p,t}^s} \sim \mathcal{N}(2\mu_{\beta_{p,t-1}^s} - \mu_{\beta_{p,t-2}^s}, \sigma_{\mu_{\beta_{p,t}^s}}^2)$$

#### Priors on mortality and standard deviation parameters

#### Prior on Person-years

$$\tilde{\underline{L}}_{0,a,t} \sim \mathcal{N}(\hat{L}_{0,a,t}, \hat{\sigma}^2_{\hat{L}_{0,a,t}})$$

$$\underline{\tilde{L}_{x,a,t}^s} \sim \mathcal{N}(\hat{L}_{x,a,t}^s, \hat{\sigma}_{\hat{L}_{0,a,t}}^2)$$

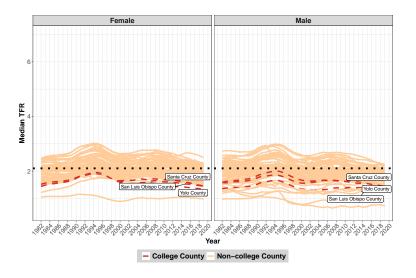
- ullet  $ilde{L}^s_{x,a,t}$  from age-, period- and sex-specific subnational life tables
- Variances calculated from the standard errors available from the subnational life tables

#### Prior on standard deviation parameters

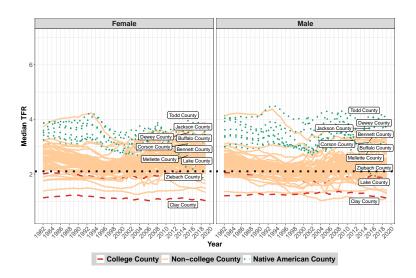
$$\sigma_{\beta_{p,a,t}^s}, \sigma_{TFR_{a,t}^s}, \sigma_{\mu_{\beta_{p,t}^s}} \sim \mathcal{N}^+(0,1)$$

weakly informative priors

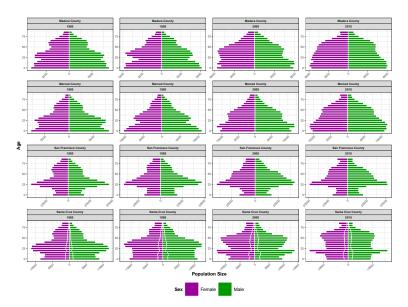
### Appendix: California TFR trajectories



### Appendix: South Dakota TFR trajectories



# Appendix: population pyramids (1)



# Appendix: population pyramids (2)

